# Iterated Even-Mansour Schemes with Involutions

<u>Itai Dinur</u><sup>1</sup>, Orr Dunkelman<sup>2,4</sup>, Nathan Keller<sup>3</sup> and Adi Shamir<sup>4</sup>

<sup>1</sup>École normale supérieure, France
<sup>2</sup>University of Haifa, Israel
<sup>3</sup>Bar-Ilan University, Israel
<sup>4</sup>The Weizmann Institute, Israel

#### The Iterated EM Scheme



- EM-based schemes are a **very hot** research area
- There are many possible key schedules

#### Involutions

- In practice the permutations F<sub>i</sub> can be constructed using a block cipher without the key schedule
- Many of these constructions have the property that they are equal to their inverses
- A permutation F is called an involution if F=F<sup>-1</sup>



#### **Fixed Points of Involutions**

- A random involution has an expected number of 2<sup>n/2</sup>
   fixed-points
- x=F(x) → F'(x)=x+F(x)=0 → the 0 output value in F'(x) has an expected number of 2<sup>n/2</sup> preimages
- When F is a random permutation the number of preimages of the most likely output is O(n)<< 2<sup>n/2</sup>

- A 2-round iterated EM scheme with 1 key can be attacked in T≈2<sup>n</sup>/t [DDKS'13]
  - t is the number of preimages of the most likely output of F'(x)=x+F(x)
- When  $F_1$  and  $F_2$  are random permutations  $T \approx 2^n/n$



- A 2-round iterated EM scheme with 1 key can be attacked in T≈2<sup>n</sup>/t [DDKS'13]
  - t is the number of preimages of the most likely output of F'(x)=x+F(x)
- When  $F_1$  and  $F_2$  are random permutations  $T \approx 2^n/n$
- When  $F_1$  (or  $F_2$ ) is a random involution  $T \approx 2^{n/2}$ 
  - The memory and data complexities are also significantly reduced

$$P_{i} \xrightarrow{F_{1}} F_{2} \xrightarrow{F_{2}} C_{i}$$

$$K \xrightarrow{K} \xrightarrow{K} \xrightarrow{K}$$

- A 3-round iterated EM scheme with 1 key can be attacked in T≈2<sup>n</sup>/Vt [DDKS'13]
- When all permutations are random T≈2<sup>n</sup>/√n



- A 3-round iterated EM scheme with 1 key can be attacked in T≈2<sup>n</sup>/Vt [DDKS'13]
- When all permutations are random T≈2<sup>n</sup>/√n
- When  $F_1$  (or  $F_2$  or  $F_3$ ) is a random involution  $T \approx 2^{3n/4}$ 
  - The memory and data complexities are also significantly reduced



#### A Surprising Application

 A 2-round iterated EM scheme with 1 key with random permutations can be attacked in T≈2<sup>n</sup>/n



### A Surprising Application

- A 2-round iterated EM scheme with 1 key with random permutations can be attacked in T≈2<sup>n</sup>/n
- Add an arbitrary involutional round (unrelated to the original permutations)



## A Surprising Application

- A 2-round iterated EM scheme with 1 key with random permutations can be attacked in T≈2<sup>n</sup>/n
- Add an arbitrary involutional round (unrelated to the original permutations)
- This **significantly reduces** the security to T≈2<sup>3n/4</sup> !!
  - Also significantly reduces the data and memory complexities of the attack



# Thank you for your attention!